

Skill Topics



Application Topics



Resources



# Math OER

## Math 52 Midterm

Name:

Date:

*Calculators **are** allowed. Notes **are** allowed.*

*Reduce fraction answers. No need to change improper fraction answers to mixed numerals.*

*Turn in a page with your own numbered step-by-step answers.*

1 - §1.1. Reduce the fraction  $\frac{6}{15}$

2 - §1.1. Reduce the fraction  $\frac{37.5}{325}$

3 - §1.2. Find  $\frac{12}{20} \div \frac{4}{5}$

4 - §1.2. Find  $\frac{27}{200} \div \frac{0.3}{20}$  (For full credit, show the two steps of fraction division.)

You may use your calculator's fraction key to reduce the answer.)

5 - §1.2. Find the sum of  $\frac{1}{4}$ ,  $\frac{1}{6}$ , and  $\frac{9}{12}$  using common denominators.

6 - §1.3. Write 20.16 as a mixed number.

7 - §2.2. Which decimal is bigger, 0.8879 or 0.8899?

8 - §2.2. Round 8328.8328 to the nearest thousandth.

9 - §2.3. Simplify:  $8,348.551 \times 10,000$

10 - §2.3. Simplify:  $8,308.531 \div 0.0001$

**11 - §2.4.** Superbia City has a population of 832,800 people and an area of 3.2 square miles. Find its population density in people per square mile.

**12 - §2.4.** Brand A costs \$33.39 for 16 ounces. Brand B costs \$31.17 for 14 ounces. What is the price per ounce for each? Which is the better buy?

**13 - §3.1.** Simplify:  $3 \times (4 + 18 \times 4) + 5 - 3 + 81 \div 3^2 \times 2^3$

**14 - §3.4.** Simplify:  $\frac{71}{14} - [2 \frac{1}{2} \times (-4 \frac{1}{3} \div -2 \frac{1}{3})]$

**15 - §4.1.** Change the temperature 50 degrees Fahrenheit into degrees Celsius.

**16 - §4.1.** Your friend is a 19-year-old very active woman who weighs 152 pounds and is 5 feet 9 inches tall. What is her estimated BMR?

**17 - §4.1.** Continuing the previous problem, what is her estimated DCI?

**18 - §4.1.** Continuing the previous problem, that same friend bicycles for 1 hour and 33 minutes. Bicycling burns 0.045 calories per pound per minute. How many calories does your friend burn? To how many 50-calorie *York Peppermint Pattie* mini-size candies is this equivalent?

**19 - §4.1.** Continuing the previous problem, what is that friend's maximum safe heart rate, minimum aerobic exercise heart rate, and maximum aerobic exercise heart rate?

**20 - §4.2.** Solve:  $60 = p \times 3$

**21 - §4.2.** Solve:  $70 \div q = 5$

**22 - §4.2.** A number divided by 108 equals 12. What is the number?

**23 - §4.2.** A number minus  $\frac{1}{45}$  equals  $\frac{1}{9}$ . What is the number?

**24 - §4.2.** Solve:  $7w = 3w + 8$

**25 - §4.4.** Check if this proportion is true or false: 4 to 21 is perhaps proportional to 24 to 126.

**26 - §4.4.** Solve:  $\frac{27}{10} = \frac{n}{27}$

**27 - §4.5.** A car drives 33 miles on 7.3 gallons of gasoline. At this rate, how many gallons are used by a 551 mile trip?

**28 - §4.5.** The vet gives Jane a 855 ounce bag of dinosaur food containing 30 milligrams of medicine. Jane needs to give her dinosaur a dose of 3.3 milligrams of medicine. How many ounces of that dinosaur food should she feed her dinosaur?

**29 - §4.5.** A college is expanding from 380 to 1,349 students. It has 20 instructors. How many more instructors must it hire to maintain its student-to-faculty ratio?

**30 - §4.5.** A rectangular image on a web page has a length of 31 pixels and a width of 64 pixels. It needs to be resized to a length of 87 pixels. What will the new width be?

**31 - §4.6.** A respiratory therapist is administering oxygen to a patient. Each tank has 1,300 mL of oxygen at a pressure of 700 mmHg. Her equipment reduces the pressure the patient receives to 300 mmHg. Use Boyle's Law to find the volume provided by each tank.

**32 - §4.7.** A graph of a line goes through the points (10, 11) and (16, 20). What is the slope of this line?

**33 - §5.1.** Write 20.551% in decimal format.

**34 - §5.1.** Write 68.38 in percent format.

**35 - §5.1.** Write the fraction  $\frac{2}{200}$  as a decimal.

**36 - §5.1.** Write the fraction  $\frac{3}{24}$  in percent format.

**37 - §5.1.** Write  $9\frac{2}{5}\%$  in fraction format.

**38 - §5.2.** What is 29% of 571?

**39 - §5.2.** 224.58 is what percent of 591?

**40 - §5.2.** 287.17 is 47% of what?

**41 - §5.2.** 22% of what is 25?

**42 - §5.2.** A certain car depreciates in value 23% during its first year. That car is worth \$11,000 after its first year. What was its original cost?

**43 - §5.2.** Sally the Wonder Snail crawls 4,320 yards in 45 days. What percentage of a mile is this distance?

**44 - §5.2.** Sterling pays for a \$967 payday loan for 30 days with a post-dated check for \$988.46. What was the loan's simple interest rate?

**45 - §5.4.** Complete this quantity-value table.

| Item         | Grams    | Grams % | Calories    | Calories % |
|--------------|----------|---------|-------------|------------|
| Fat          | 14 grams |         |             |            |
| Carbohydrate |          |         | 76 calories |            |
| Protein      | 5 grams  |         |             |            |

Show Answers

**1 - §1.1.** Divide both top and bottom by 3 to get  $\frac{2}{5}$

**2 - §1.1.** First multiply both top and bottom by 10 to get  $\frac{375}{3250}$ .

Then divide both top and bottom by 125 to get  $\frac{3}{26}$

**3 - §1.2.** First flip the second fraction change division to multiplication:  $\frac{12}{20} \times \frac{5}{4}$

Then cancel the top right and bottom left:  $\frac{3}{20} \times \frac{5}{1}$

Then cancel the bottom right and top left:  $\frac{3}{4} \times \frac{1}{1}$

Then multiply the fractions to find the final answer of  $\frac{3}{4}$ .

**4 - §1.2.** Do fraction division by flipping the second fraction and multiplying:  $\frac{540}{60}$ . Then reduce to get  $\frac{9}{1}$ .

**5 - §1.2.** The common denominator is 12. We add  $\frac{3}{12} + \frac{2}{12} + \frac{9}{12}$   
 $= \frac{14}{12}$ . The reduced fraction is  $\frac{7}{6}$ .

**6 - §1.3.** The whole number 20 just hangs out in front as a whole number. The decimal part is 16 *hundredths* so we write it as the fraction  $\frac{16}{100}$ . Then simplify the fraction part by dividing top and bottom by 4 to get **20  $\frac{4}{25}$** .

**7 - §2.2.** the second number, **0.8899**

**8 - §2.2.** **8328.833**

**9 - §2.3.** 4 scoots to the right gives an answer of **83,485,510**

*Note: The previous problem is sometimes displayed wrong due to floating point arithmetic.*

**10 - §2.3.** 4 scoots to the right gives an answer of **83,085,310**

**11 - §2.4.** Rounding to the nearest whole number gives us **260,250 people per square mile.**

**12 - §2.4.** Brand A costs \$2.09 per ounce. Brand B costs \$2.23 per ounce. **Brand A** is the better buy.

**13 - §3.1.** The amount in the parenthesis simplifies to 76. So the first term is  $3 \times 76 = 228$ .

The second and third terms are plain numbers: add 5 and subtract 3.

The fourth term involves two exponents. The first part becomes  $81 \div 9 = 9$ . The second exponent equals 8. Then  $9 \times 8 = 72$ .

Thus the entire list of terms is  $228 + 5 - 3 + 72 = 302$ .

**14 - §3.4.** The inner parenthesis becomes  $\frac{13}{7}$  and then the bracket amount becomes  $\frac{65}{14}$ . The final subtraction step results in  $\frac{6}{7}$

**15 - §4.1.** To change from Fahrenheit to Celsius we use the formula  $C = (F - 32) \div 1.8$ . So 50 degrees Fahrenheit becomes about **10.0 degrees Celsius**.

**16 - §4.1.** A woman's BMR = (weight  $\times$  4.55) + (height  $\times$  15.88) - (age  $\times$  5) + 5  
=  $(152 \times 4.55) + (69 \times 15.88) - (19 \times 5) + 5 \approx$  **1,697 calories per day**.

**17 - §4.1.** The DCI for a very active woman is  $BMR \times 1.82 \approx$  **3,089 calories per day**.

**18 - §4.1.**  $0.045 \times 152$  pounds  $\times$  93 minutes  $\approx$  **636 calories**, equivalent to about 13 *York Peppermint Pattie* mini-size candies.

**19 - §4.1.** Our friend's maximum safe heart rate =  $211 - (0.64 \times \text{age}) = 211 - (0.64 \times 19) =$  **199 beats per minute**. The upper limit for aerobic exercise = maximum safe heart rate  $\times$  0.85  $\approx$  **169 beats per minute**. The lower limit for aerobic exercise = maximum safe heart rate  $\times$  0.5  $\approx$  **99 beats per minute**

**20 - §4.2.** Divide both sides by 3 to get  $p = 20$

**21 - §4.2.** Divide both sides by 5 to get  $q = 14$

**22 - §4.2.** Rewrite the word problem as the equation  $z \div 108 = 12$ . To get  $z$  by itself we multiply both sides by 108. The answer is **1296**.

**23 - §4.2.** First notice that 45 will work as a common denominator. So change the second fraction to get  $\frac{1}{45} + \frac{5}{45}$ . Then add numerators to get  $\frac{6}{45}$ . The reduced fraction is  $\frac{2}{15}$ .

**24 - §4.2.** Subtract  $3w$  from both sides. We get  $4w = 8$ . Divide both sides by 4 to get  $w = 2$ .

**25 - §4.4.** The cross products are  $4 \times 126 = 504$  and  $21 \times 24 = 504$ . The proportion is **true**.

**26 - §4.4.**  $n = 27 \times 27 \div 10 \approx 72.9$

**27 - §4.5.** The trip will use **121.9 gallons**.

**28 - §4.5.** There are  $855 \div 30 = 28.5$  ounces of dinosaur food for each milligram of medicine. So Jane needs to give her dinosaur about  $3.3 \times 28.5 = 94$  **ounces** of dinosaur food.

**29 - §4.5.** The old faculty-to-student ratio is  $380 \div 20 = 19$ . The number of students is increasing by 969. So the college must hire  $969 \div 19 = 51$  **more instructors**.

**30 - §4.5.** The scale factor is 2.8, so the new width will be **179 pixels**.

**31 - §4.6.** The product of the tank's volume and pressure is  $1,300 \text{ mL} \times 700 \text{ mmHg} = 910,000$ , so the new volume will be that product divided by the new pressure of 300 mmHg, resulting in **3033 mL**.

**32 - §4.7.** The difference in Y coordinates is 9 and the difference in X coordinates is 6. We divide to find the slope of **1.50**.

**33 - §5.1.** Use RIP LOP and scoot the decimal point twice to the left to get **0.20551**

**34 - §5.1.** Use RIP LOP and scoot the decimal point twice to the right to get **6,838%**

**35 - §5.1.** Do "top  $\div$  bottom" to get **0.01**.

**36 - §5.1.** First change the fraction into a decimal by using **top  $\div$  bottom** to get 0.125, then use RIP LOP and scoot the decimal point twice to the right to get **12.5%**

**37 - §5.1.** First change the mixed number into an improper fraction, still in percent format:  $\frac{47}{5} \%$ . Then replace the **%** symbol with  $\times \frac{1}{100}$  and multiply. The result is  $\frac{47}{500}$ . Reduce if necessary. The answer is  $\frac{47}{500}$ .

**38 - §5.2.** Translate the percent sentence as  $y = 0.29 \times 571 = 165.59$ .

**39 - §5.2.** Translate the percent sentence as  $224.58 = y \times 591$ . Solve for  $y$  by dividing both sides by 591. The answer is **38%**.

**40 - §5.2.** Translate the percent sentence as  $287.17 = 0.47 \times y$ . Solve for  $y$  by dividing both sides by 0.47. The answer is **611**.

**41 - §5.2.** Translate the percent sentence as  $0.22 \times y = 25$ . Solve for  $y$  by dividing both sides by 0.22. The answer is about **113.64**.

**42 - §5.2.** Change the word problem into a percent sentence by asking *\$11,000 is 77% of what?* Then translate the percent sentence as  $11,000 = 0.77 \times y$ . Solve for  $y$  by dividing both sides by 0.77 to get an answer of **\$14,286**.

**43 - §5.2.** First multiply by 3 to change the distance to 12,960 feet. Then divide by 5,280 to find the fraction of a mile. The answer is about 2.455 miles. Finally, use RIP LOP to change the decimal into percent format. The rounded answer is **245% of a mile**.

**44 - §5.2.** Use the simple interest formula.

$$I = P \times r \times t = \$21.46 = \$967 \times r \times (30 \div 365)$$

We can isolate the rate by dividing by \$967 and then dividing by  $(30 \div 365)$ .

Then we use RIP LOP to turn the decimal value into percent format.

Our final answer is  $r = 27\%$ .

**45 - §5.4.** Here is the completed table.

| Item         | Grams       |     | Calories        |     |
|--------------|-------------|-----|-----------------|-----|
|              | Grams       | %   | Calories        | %   |
| Fat          | 14<br>grams | 37% | 126<br>calories | 57% |
| Carbohydrate | 19<br>grams | 50% | 76<br>calories  | 34% |
| Protein      | 5 grams     | 13% | 20<br>calories  | 9%  |